

# Lecture outline

- Feedback loops in behavioral dynamics

# Behavioral dynamics

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- How did you make decisions?
  - » What was your thought process?
  
  - » How would you classify your decision-making progress in terms of the four types of policies introduced earlier?
    - Myopic policy
    - Lookahead
    - Policy function approximation (which kind?)
    - Policy based on value function approximation

# Behavioral dynamics

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- A common policy structure is called **anchor** and **adjustment**:
  - » **Anchor**: A fixed action, possibly based on a *plan* (a set of actions based on a particular set of future events or an expected system state).
  - » **Adjustment**: Changes made to the “anchor” based on deviations from planned future events or deviation from an expected system state.

# Behavioral dynamics

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## ■ What information did we have?

Physical state:

$R(t)$  = Current inventory (or backorder if  $R_t < 0$ ) at time  $t$

Activity variables:

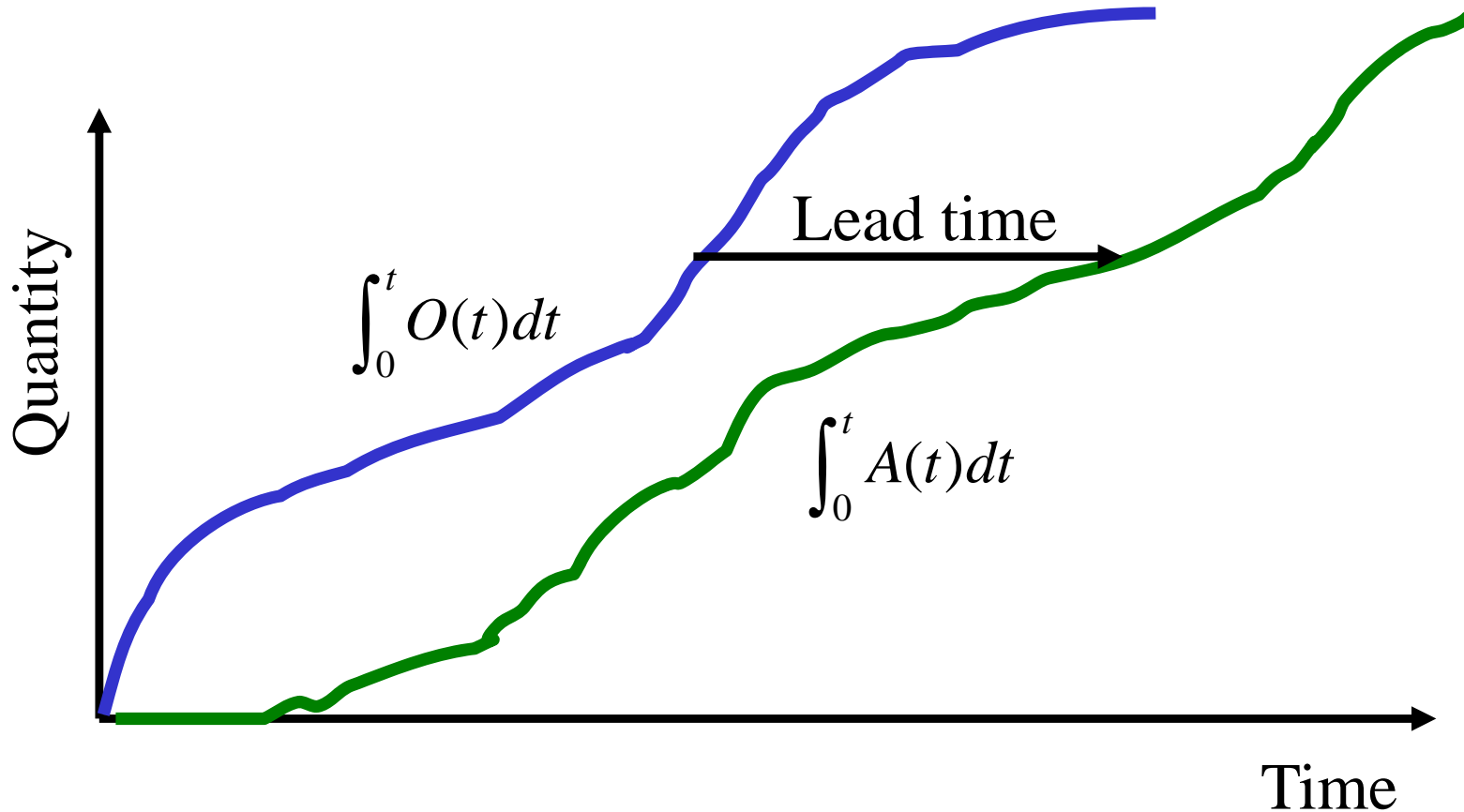
$A(t)$  = Arrival rate

$L(t)$  = Loss rate

$O(t)$  = Order rate

$R^{transit}(t)$  = In-transit inventory (inbound)

# Behavioral dynamics



$$R(t) = \int_0^t (A(t) - L(t)) dt + R(0) = \text{Current inventory}$$

$$R^{transit}(t) = \int_0^t (O(t) - A(t)) dt + R^{transit}(0) = \text{Supply line}$$

# Behavioral dynamics

## ■ Observation:

- » If there was no lead time (and no fixed order cost), what would you do?

$$\begin{aligned}\tilde{O}(t) &= \text{"Indicated order rate" (how much you should order)} \\ &= L(t-1) \quad (\text{i.e. order what you lost in the previous time period})\end{aligned}$$

- » Why would you do otherwise?
  - Uncertainties in order lead times?
  - Need to build up larger buffer inventory?
  - Anticipation of higher demand?
  - Current stock under/over what you think you need?

*We need to make “adjustments” to our basic model.*

# Behavioral dynamics

## ■ Refining our model:

- » Behavioral strategy - anchor and adjustment (Tversky)
  - Anchor - Create a known reference point
  - Adjustment - Change based on position relative to the anchor.

» Let:

$$\tilde{L}(t) = \text{Perceived loss rate}$$

$$\delta R(t) = \text{Adjustment to order based on current stock.}$$

$$\delta R^{transit}(t) = \text{Adjustment to order based on current supply line.}$$

» New behavioral model:

$$\tilde{O}(t) = \tilde{L}(t) + \delta R(t) + \delta R^{transit}(t)$$

» Since this may be negative, our new ordering model is:

$$O(t) = \left[ \tilde{O}(t) \right]^+$$

# Behavioral dynamics

## ■ Calculating the perceived loss rate:

» Possible models:

Reactive:

$$\tilde{L}(t) = L(t-1) \quad \text{Perceived loss equal to last period's actual loss.}$$

Stable:

$$\tilde{L}(t) = L^* \quad \text{Equal to a constant}$$

Regressive expectations

$$\tilde{L}(t) = \gamma L(t-1) + (1-\gamma)L^*$$

Adaptive:

$$\tilde{L}(t) = (1-\gamma)\tilde{L}(t-1) + \gamma L(t-1)$$



# Behavioral dynamics

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## ■ Adjustments:

» For current stock:

$$\delta R(t) = \alpha (R^* - R(t))$$

where:

$\alpha$  = damping factor.

$R^*$  = desired stock level (in itself a function)

$R(t)$  = current stock

» What is  $R^*$  a function of?

# Behavioral dynamics

## ■ Adjustments:

» For supply line:

$$\delta R^{transit}(t) = \alpha_{SL} \left( R^{transit*}(t) - R^{transit}(t) \right)$$

where:

$\alpha_{SL}$  = damping factor for the supply line.

$R^{transit*}(t)$  = desired supply line level (in itself a function).

$R^{transit}(t)$  = current supply line.

The target supply line might be:

$$R^{transit*}(t) = T^{lag}(t) P^*(t)$$

where:

$T^{lag}(t)$  = estimated time lag between order and arrival.

$P^*(t)$  = desired product throughput.

# Behavioral dynamics

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## ■ Observation:

- » Anchoring and adjustment is an exceptionally powerful model.
- » General method:
  - Find an anchor by solving a simple version of the problem
  - Develop adjustment mechanisms based on available information.
- » Examples:
  - What quantity to order (product, investment, energy storage)?
    - Anchor – based on expectation
    - Adjustment – over time, build up an idea of safety stock